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New families of scale separated vacua

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String Phenomenology, Padova, June 27, 2024

Based on [2309.00043](#) [R. Carrasco, TC, F. Marchesano and D. Prieto] and review
[2311.12105](#) [TC]

Hiding the extra dimensions

10d spacetime =



4d world

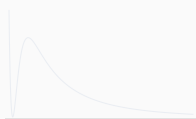
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Compact X^6

- Cosmological constant Λ

$$\Rightarrow R_{(\Lambda)\text{dS}} M_{\text{p}} \sim |\Lambda|^{-1/2}$$



- Kaluza-Klein scale $M_{\text{KK}} \sim \frac{M_{\text{s}}}{\text{Vol}_{X^6}^{1/6}}$ (and winding scale)

Scale separation: $R_{(\Lambda)\text{dS}} M_{\text{KK}} \gg 1$

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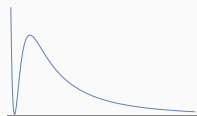
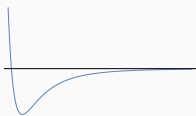
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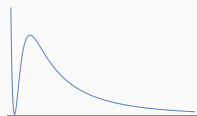
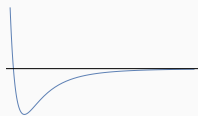
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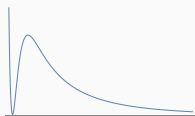
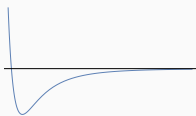
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- $X_6 = T^6 / (\mathbb{Z}_3 \times \mathbb{Z}_3) \implies h^{2,1} = 0$ & let us forget twisted moduli

$$t^a \propto \frac{\sqrt{|\hat{e}_1 \hat{e}_2 \hat{e}_3|}}{|\hat{e}_a| \sqrt{m}} \quad \text{with} \quad \hat{e}_a \equiv e_a - \frac{1}{2} \frac{\mathcal{K}_{abc} m^b m^c}{m}$$

Tadpole: $dG_2 = G_0 H + Q_{O6} \delta_{O6}$

\implies Flux quanta e_a, m^a unconstrained

$$\hat{e}_a \sim n$$

$$t^a \sim n^{\frac{1}{2}}, \quad \text{Vol}_{X_6} \sim n^{\frac{3}{2}}, \quad e^\phi \propto (\mathcal{K}_{abc} t^a t^b t^c)^{-\frac{1}{2}} \sim n^{-\frac{3}{4}}, \quad e^{\phi_4} \sim n^{-\frac{3}{2}}$$

Good control: $n \rightarrow \infty \implies$ large volume/weak coupling

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$$R_{\text{AdS}} M_{\text{KK}} \sim n^{\frac{1}{2}}, \quad \text{and} \quad R_{\text{AdS}} M_{\text{W}} \sim n$$

Susy AdS:

- Moduli stabilised
- Controlled regime
- Scale separation
- Pert. stable

Generalisable:

- Metric fluxes [Camara, Font, Ibáñez '05]
- [Derendinger, Kounnas, Petropoulos, Zwirner '05] [Villadoro, Zwirner '05]
- Arbitrary CY, Non-susy [Narayan, Trivedi '10]
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Status of scale separation



Status of scale separation [DeWolfe, Giryavets, Kachru, Taylor '05]



Status of scale separation [Banks, van den Broek '07][McOrist, Sethi '12]

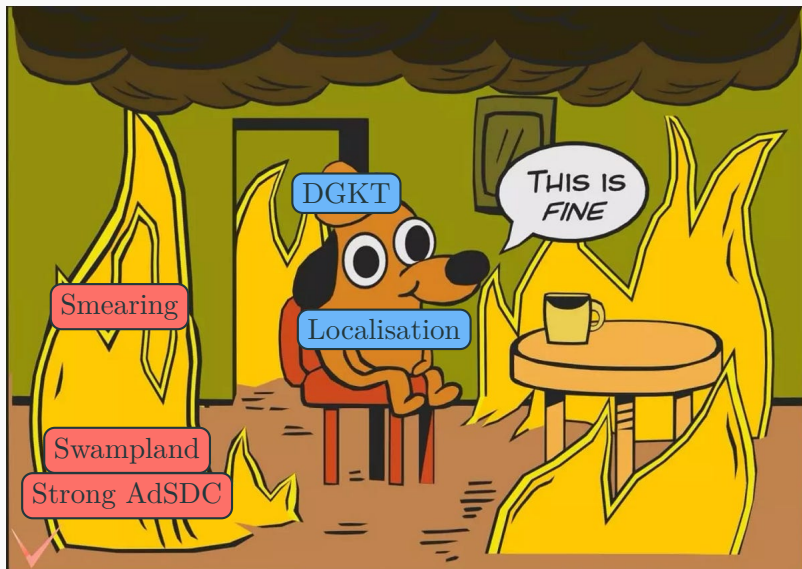


Status of scale separation [Junghans '20]

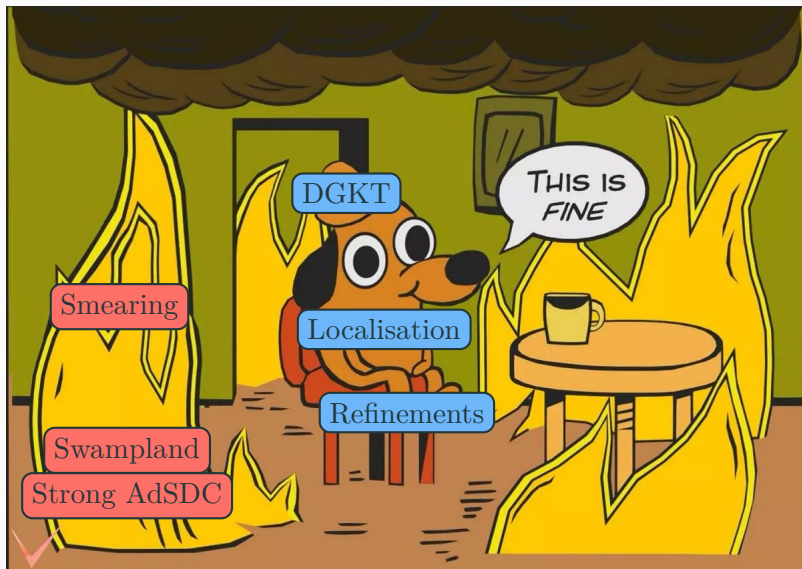
[Marchesano, Palti, Quirant, Tomasiello '20]



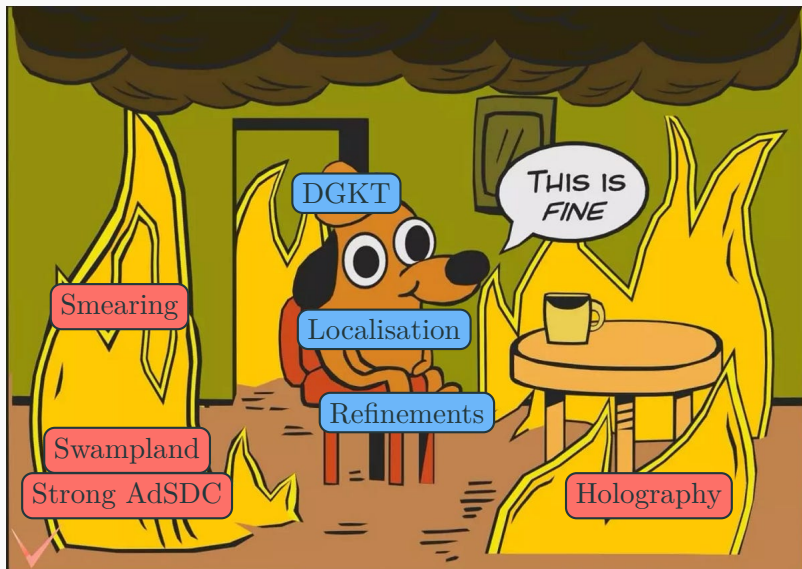
Status of scale separation [D. Lust, Palti, Vafa '19]



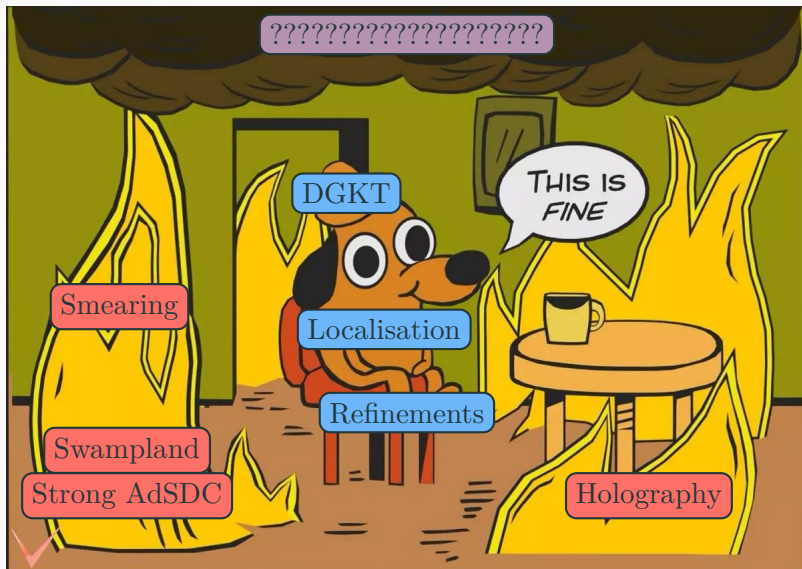
Status of scale separation [Buratti, Calderon, Mininno, Uranga '20]



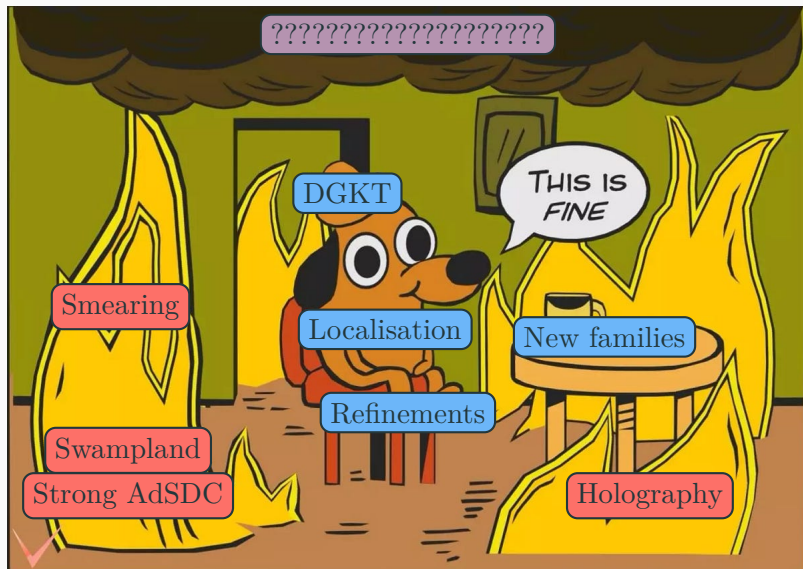
Status of scale separation [Polchinski, Silverstein '09] [Montero, Rocek, Vafa '23] [Collins, Jafferis, Vafa, Xu, Yau '22] [Apers, Conlon, Ning, Revello '22] ...



Status of scale separation



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New families: Double T-duality [Banks, Van Den Broek '06]

- We consider $(T^2)^3/\Gamma$

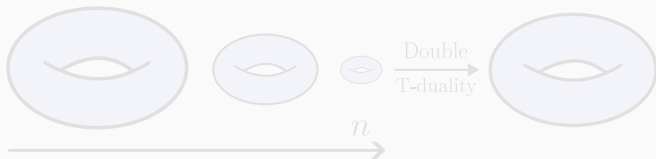
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Can be satisfied even when $s < 0 \iff$ shrinking torus factor



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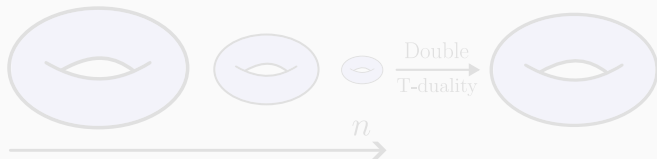
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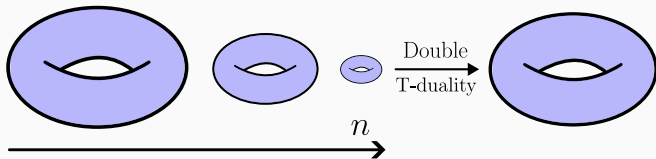
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Where T-duality brings us

- $K_K = -\log \left(i\kappa(T^1 - \bar{T}^1)(T^2 - \bar{T}^2)(T^3 - \bar{T}^3) \right), \quad \kappa = \mathcal{K}_{123}$
- $K_Q(\mathcal{P}^a)$

Double T-duality for $a = 1$: $T^1 \mapsto -\frac{1}{T^1}$

$$K_K \mapsto K_K + \log |T^1|^2$$

Kähler transf.: $K_K \mapsto K_K - F - \bar{F}, W \mapsto e^F W, \quad F = \log T^1$

$$W_{RR} = e_0 + e_a T^a + \frac{1}{2} \mathcal{K}_{abc} m^a T^b T^c + \frac{m}{6} \mathcal{K}_{abc} T^a T^b T^c$$



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$$\begin{array}{c} W_{\text{NS}} = h_{\mu} U^{\mu} \\ \downarrow \\ W_{\text{NS}} = h_{\mu} U^{\mu} T^1 \end{array}$$

- Quadratic term mixing U^{μ} and T^1

H-flux \mapsto Metric fluxes (rank-one)

Lost Romans mass but price to pay: Depart from CY

Back to 4d setup

$$W_{\text{RR}}, W_{\text{NS}} = h_\mu U^\mu + f_{a\mu} T^a U^\mu$$

$f_{a\mu} \in \mathbb{Z} \longleftrightarrow$ metric fluxes:

$$d\omega_a = -f_{a\mu} \beta^\mu, \quad d\alpha_\mu = -f_{a\mu} \tilde{\omega}^a$$

Tadpole: $[m^a f_{a\mu} + m h_\mu + m f_{a\mu} b^a] \beta^\mu + N_\alpha \delta_{\text{D6}}^\alpha - 4\delta_{\text{O6}} = 0$

$\implies e$ fluxes (G_4 and G_6) are not constrained
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Generalizes the toroidal construction of [Cribiori, Junghans, Van

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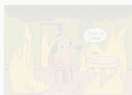
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- Status **uncertain** in string theory



→ Progress on source localisation and past worries

→ Bottom-up constructions **clashes** with Swampland and holography

- We proposed new families of sol. in massless type IIA

→ More details right now!

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