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Geometry of orientifold vacua with broken supersymmetry

Thibaut Coudarchet Instituto de Física Teórica UAM-CSIC Iberian Strings, Gijón, March 24, 2022

Based on 2105.06913, TC, E. Dudas and H. Partouche

• <u>Scherk-Schwarz mechanism</u> [Scherk, Schwarz, '79] [Rhom, '84] [Ferrara, Kounnas, Porrati, Zwirner, '89] [Kounnas, Rostand, '90]

Spacetime $\mathbb{R}^{1,3} \times S^1(R) \longrightarrow \phi(x, y + 2\pi R) \equiv \phi(x, y)$

Symmetry $T = e^{i\pi Q} \longrightarrow \phi(x, y + 2\pi R) \equiv e^{i\pi Q}\phi(x, y)$

$$\phi(x,y) = \sum_{m \in \mathbb{Z}} \phi_m(x) e^{\frac{i\left(m + \frac{Q}{2}\right)y}{R}} \longrightarrow M_{\phi_m(x)} = \frac{\left|m + \frac{Q}{2}\right|}{R}$$

Q = fermion number $F \Longrightarrow$ SUSY breaking

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• Brane supersymmetry breaking (BSB) [Sugimoto, '99] [Antoniadis,

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Models with SUSY closed sector

Breaking only visible in the Möbius amplitude

Non-mutually BPS D-branes and O-planes

Global tension not zero \implies NS-NS tadpoles!

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Start from a SUSY model with O_- and O_+ -planes

Replace an O_- - O_+ pair by an \overline{O}_- - \overline{O}_+ pair

Unchanged charge and tension \Longrightarrow No R-R or NS-NS tadpoles

Link between geometry and amplitudes

Amplitudes $\mathcal{K}, \mathcal{A}, \mathcal{M} \xrightarrow{S \text{ transformation}} =$ Closed-string channel $\tilde{\mathcal{K}}, \tilde{\mathcal{A}}, \tilde{\mathcal{M}}$

Closed-string states propagation between D-branes and/or O-planes

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In 8d, $\mathbb{R}^{1,7} \times S^1(R_8) \times S^1(R_9)$ D9-branes and O9_-plane $\xrightarrow{\text{T-duality}}$ D7-branes and 4 O7_-planes



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 $(X^8, X^9) \stackrel{\Omega'}{\longrightarrow} (-X^8, -X^9)$

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Amplitude from geometry: $\tilde{\mathcal{K}}$

 $\begin{array}{c} \text{O-plane} & - \text{Closed-string propagator} & - \text{O-plane} \\ A & \text{NS-NS or RR} & B \end{array}$ KK wave functions multiplied by phases $e^{i \vec{m} \cdot (\vec{x}_A - \vec{x}_B)}$ NS-NS: $T_A T_B V_8$ RR: $q_A q_B S_8$



 $\tilde{\mathcal{K}} \supset 4[1 + (-1)^{m_9}][1 + (-1)^{m_8}]P_{m_8}P_{m_9}\frac{V_8 - S_8}{\eta^8}$

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Rank 8 type IIB orientifold theory









SUSY breaking model



The Klein bottle remains SUSY

The annulus also

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Gauge group USp(16) Gauge-singlet goldstino

 \implies Nonlinear realization of supersymmetry

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 $\left. \mathcal{A} + \mathcal{M} \right|_0 \supset \frac{N(N+1)}{2} \left. \frac{V_8}{\eta^8} \right|_0 - \frac{N(N-1)}{2} \left. \frac{S_8}{\eta^8} \right|_0$

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 \implies Nonlinear realization of supersymmetry

SUSY Klein bottle \implies SUSY closed-string spectrum? [Angelantonj, Cardella, '04]

Torus cannot be the SUSY one:

• Consistency with geometry. Orientifold: $\Omega'' = \Omega'(-\delta_{w_9})^F$

 δ_w : Winding shift δ_p : Momentum shift

• Quantized $B_{ab} \iff$ Freely-acting orbifold $g = \delta_{w_8} \delta_{p_9}$

 $g \longrightarrow g' = (-1)^F g \Longrightarrow$ Soft breaking Scherk-Schwarz-like

 $X^9 \longrightarrow X^9 + (-1)^F 2\pi R_9 \Longrightarrow \text{O-planes at } X_9 = 0$ $\overline{\text{O-planes at }} X_9 = \pi R_9$ SUSY Klein bottle \implies SUSY closed-string spectrum? [Angelanton], Cardella, '04]

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Supersymmetric limits

SUSY restored in torus when $\left\{ \right.$

$$R_8 \to 0$$
$$R_9 \to +\infty$$

 $R_8 \rightarrow 0$: open sector also becomes SUSY

Small $R_8 \implies$ Spontaneous breaking similar to Scherk-Schwarz

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- A SUSY-breaking realization with O_{\pm} , \overline{O}_{\pm} and regular branes
- \bullet Share properties with BSB \longrightarrow Avoid NS-NS tadpoles
- \bullet Share properties with Scherk-Schwarz \longrightarrow Annulus untouched
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Thank you for your attention!

And bon appétit :)